# **Rossmoyne Senior High School**

# WA Exams Practice Paper D, 2015 Question/Answer Booklet

# MATHEMATICS METHODS UNIT 1

Section One: Calculator-free

If required by your examination administrator, please place your student identification label in this box

| Student Number: | In figures  |      |      |      |      |
|-----------------|-------------|------|------|------|------|
|                 | In words _  | <br> | <br> | <br> | <br> |
|                 | Your name _ | <br> |      | <br> | <br> |

## Time allowed for this section

Reading time before commencing work: five minutes Working time for this section: fifty minutes

## Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet Formula Sheet

#### To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: nil

#### Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

### Structure of this paper

| Section                                | Number of<br>questions<br>available | Number of questions to be answered | Working time (minutes) | Marks<br>available | Percentage of exam |  |
|--|-------------------------------------|------------------------------------|------------------------|--------------------|--------------------|--|
| Section One:<br>Calculator-free        | 8                                   | 8                                  | 50                     | 52                 | 35                 |  |
| Section Two:<br>Calculator-<br>assumed | 13                                  | 13                                 | 100                    | 98                 | 65                 |  |
|  |                                     |                                    | Total                  | 150                | 100                |  |

#### Instructions to candidates

- 1. The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2015. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
     Fill in the number of the question that you are continuing to answer at the top of the page.
- 5. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

3

**METHODS UNIT 1** 

#### **Section One: Calculator-free**

(52 Marks)

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

Question 1 (5 marks)

(a) Solve 
$$2x = 5x^2$$
.

(2 marks)

(b) Solve 
$$(x-3)(x+2) = 4x$$
.

(3 marks)

Question 2 (4 marks)

(a) Evaluate  $\frac{12!}{5! \times 8!}$ .

(2 marks)

(b) Determine the sum of  $\binom{6}{0} + \binom{6}{1} + \binom{6}{2} + \binom{6}{3} + \binom{6}{4} + \binom{6}{5} + \binom{6}{6}$ . (2 marks)

Question 3 (7 marks)

(a) A line has equation 5x + 2y = 8. What is the gradient of this line?

(1 mark)

(b) Is the line 3x + y = 0.5 parallel, perpendicular, or neither, to the line 3x + y = -2?

Justify your answer. (1 mark)

- (c) Two points have coordinates P(5, -8) and Q(11, -20).
  - (i) Determine the coordinates of the mid-point of P and Q.

(1 mark)

(ii) If Q is the mid-point of P and R, determine the coordinates of R. (2 marks)

(iii) Find the equation of the straight line passing through P and Q.

(2 marks)

## Question 4 (7 marks)

- (a) A quadratic function is given by  $f(x) = (x+1)^2 4$ . For this function, determine
  - (i) the coordinates of the y-intercept.

(1 mark)

(ii) the equation of the line of symmetry.

(1 mark)

(iii) the coordinates of the turning point.

(1 mark)

- (b) Another quadratic function is given by  $y = 2 + 1.75x 0.25x^2$ . Determine
  - (i) the equation of the line of symmetry.

(1 mark)

(ii) the coordinates of the x-intercepts.

(3 marks)

Question 5 (8 marks)

- (a) A function is defined as f(x)=10-2x over the domain  $\{x:x=1, 3, 5\}$ . Determine the range of f(x). (1 mark)
- (b) State the natural domain and corresponding range for the function  $g(x) = 4 \sqrt{x+3}$ . (2 marks)
- (c) The function h is given by  $h(x) = 2(x+3)^2 1$ .
  - (i) Determine the x-coefficient of the expanded form of this polynomial. (1 mark)
  - (ii) State the range of the graph of y = 3h(x). (1 mark)
- (d) Comment on the behaviour of the following graphs as  $x \rightarrow -\infty$ .

(i) 
$$y = x^5$$
. (1 mark)

(ii) 
$$y = x^{-1}$$
. (1 mark)

(iii) 
$$y = \sqrt{2-x} . ag{1 mark}$$

Question 6 (8 marks)

- (a) A polynomial is given by  $5-x+2x^2-4x^3+x^4$ .
  - (i) State the degree of this polynomial.

(1 mark)

(ii) Determine the sum of all the coefficients of this polynomial.

(1 mark)

- (b) A row of Pascal's triangle starts with the numbers 1, 5, 10, ...
  - (i) Write down the numbers that complete the row.

(1 mark)

(ii) Express the sum of all the numbers in the row as a power of 2.

(1 mark)

(iii) Expand  $(2x-1)^5$ .

(4 marks)

Question 7 (6 marks)

(a) Determine the exact value of  $\tan\left(-\frac{\pi}{3}\right)$ .

(1 mark)

(b) Solve  $\sin^2(x) - \sin(x) = 2$  for  $0 \le x \le 360^\circ$ .

(3 marks)

(c) Using the identity  $\cos(x - y) = \cos(x) \cdot \cos(y) + \sin(x) \cdot \sin(y)$  and the substitutions x = 90 - A and y = B show that  $\sin(A + B) = \sin(A) \cdot \cos(B) + \cos(A) \cdot \sin(B)$ . (2 marks)

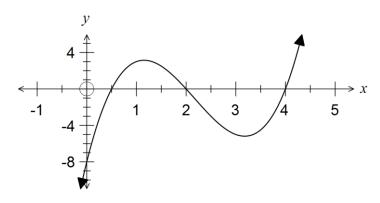
**Question 8** 

(7 marks)

(a) Expand (2x+1)(x+1)(2x-1).

(2 marks)

(b) The graph of  $y=2x^3-13x^2+22x-8$  is shown below.



Factorise  $2x^3 - 13x^2 + 22x - 8$ .

(2 marks)

(c) Solve  $x^3 - 2x^2 - 5x + 6 = 0$ .

(3 marks)

| Add | itional | working | space |
|-----|---------|---------|-------|
| Auu | itionai | Working | Space |

Question number: \_\_\_\_\_

| This examination paper may be freely copied, or communicated on an intranet, for non-commercial purposes within educational institutes that have purchased the paper from WA Examination Papers provided that WA Examination Papers is acknowledged as the copyright owner. Teachers within Rossmoyne Senior High School may change the paper provided that WA Examination Paper's moral rights are not infringed. |
|--|
| Copying or communication for any other purposes can only be done within the terms of the Copyright Act or with prior written permission of WA Examination papers.  |
| Published by WA Examination Papers PO Box 445 Claremont WA 6910  |
|  |
|  |
|  |
|  |
|  |